

From (5),

$$i_o = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} V_{in} \sqrt{\frac{8 I_D}{\mu_n C_{ox} \frac{W}{L}} - V_{in}^2}$$

$$V_{GS} = \frac{V_{GS1} + V_{GS2}}{2} \Leftarrow \text{DC-Bias of NMOS voltage}$$

$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{th})^2$$

apply

$$\Rightarrow i_o = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} V_{in} \sqrt{4(V_{GS} - V_{th})^2 - V_{in}^2}$$

$$= \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{th}) V_{in} \sqrt{1 - \frac{V_{in}^2}{4(V_{GS} - V_{th})^2}}$$

$$\text{if } V_{in} \ll 2(V_{GS} - V_{th})$$

$$\downarrow \sqrt{1-x} \approx 1 - \frac{x}{2}$$

$$\approx \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{th}) V_{in} \left(1 - \frac{V_{in}^2}{8(V_{GS} - V_{th})^2} \right)$$

$$= \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{th}) \left(V_{in} - \frac{1}{8(V_{GS} - V_{th})^2} V_{in}^3 \right)$$

$$\Rightarrow \alpha_1 = g_m = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{th})$$

$$\alpha_2 = 0$$

$$|\alpha_3| = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{th}) \frac{1}{8(V_{GS} - V_{th})^2}$$