

(3)

$$\overline{i_{nch}}^2 = 4KT \delta g_{do} \left(\frac{\omega C_{gs}}{\sqrt{5} g_{do}} \right)^2 \Delta f$$

$$= 4KT \delta \left(\frac{g_m}{\alpha} \right) \left(\frac{\omega C_{gs}}{\sqrt{5} (g_m/\alpha)} \right)^2 \Delta f$$

$$= 4KT \alpha \cdot \delta \cdot g_m \left(\frac{\omega C_{gs}}{\sqrt{5} g_m} \right)^2 \Delta f \Rightarrow \text{another expression in terms of } g_m.$$

NOTE) - Drain thermal noise current and induced gate noise are originated from same source.

- The two noise sources can thus be expected to be correlated.

- They are completely correlated?

No, because of the capacitive coupling there is only a partial correlation.

Let's separate $\overline{i_{nch}}$ into correlated and non-correlated part to drain noise current.

$$\overline{i_{nch}}^2 = 4KT \delta g_{do} \left(\frac{\omega C_{gs}}{\sqrt{5} g_{do}} \right)^2 (1 - |c|^2) \Delta f \Rightarrow \text{uncorrelated part}$$

$$+ 4KT \delta g_{do} \left(\frac{\omega C_{gs}}{\sqrt{5} g_{do}} \right)^2 |c|^2 \Delta f \Rightarrow \text{correlated part}$$

$$= 4KT \delta g_g (1 - |c|^2) \Delta f + 4KT \delta g_g |c|^2 \Delta f$$

$$\text{where, } g_g = \frac{\omega^2 C_{gs}^2}{5 g_{do}} = \alpha \frac{\omega^2 C_{gs}^2}{5 \cdot g_m} = \alpha g_m \left(\frac{\omega^2 C_{gs}^2}{5 g_m^2} \right)$$

$$C = \frac{\overline{i_{nch}} \cdot \overline{i_{nd}}}{\sqrt{\overline{i_{nch}}^2 \cdot \overline{i_{nd}}^2}} \approx 0.395$$

$$= \alpha g_m \left(\frac{1}{\sqrt{5}} \frac{\omega}{\omega_T} \right)^2$$