Circuit Analysis
of Circuits Containing Diodes
Definition of Diode
Current and Voltage

• **Forward Bias**
  ▫ When $I_D > 0\text{mA}$ and $V_D > 0\text{V}$

• **Reverse Bias**
  ▫ When $I_D < 0\text{mA}$ and $V_D < 0\text{V}$
Three Analysis Techniques

- Calculations Using Ideal Diode Equation
  - Will be covered in more depth in Electronic Devices (Year 3)
- Load Line Analysis
  - Calculations from Thévenin and Norton equivalent circuits.
- Apply Piecewise Model
Example

![Circuit Diagram]

- **Vin**: 5V
- **R1**: 1k
- **D1**: d1n4002
Approach 1: Ideal Diode Equation

1. Define the diode voltage and current.
2. Write the appropriate set of equations.
3. Determine (usually given)
   a) ambient temperature
   b) reverse saturation current and
   c) ideality factor
4. Add in the ideal diode equation.
5. Solve for the diode current and voltage.
\[-5V + R1 \cdot I_D + V_D = 0\]

\[I_D = I_S \left( \frac{qV_D}{e^{nkT}} - 1 \right)\]

\[I_S = 14.1\text{nA} \text{ and } n = 1.98 \text{ for a D1N4002}\]

Assume room temperature (300K) if not specified.

\[I_D = 14.1\text{nA} \left( \frac{V_D}{e^{51.3mV}} - 1 \right)\]

\[-5V + 1k\Omega \cdot 14.1\text{nA} \left( \frac{V_D}{e^{51.3mV}} - 1 \right) + V_D = 0\]

\[V_D = 0.648V \text{ and } I_D = 4.35mA\]
Approach 2: Load Line Analysis

1. Define the diode voltage and current.
2. Obtain the I-V characteristic for the diode.
3. Determine the open circuit voltage, $V_{OC}$.
   This is the maximum voltage that could possibly be dropped across the diode.
   Find it by replacing the diode with an open and calculate the voltage drop, $V_D$.
4. Determine the short circuit current, $I_{SC}$.
   This is the maximum current that could possibly flow through the diode.
   Find it by replacing the diode with a short and calculate the current, $I_D$.
5. Plot $V_{OC}$ and $I_{SC}$ on the graph.
   Draw a line between them.
   The intersection of the load line with the I-V of the diode is the operating point of the diode.
Open Circuit Voltage

\[ V_{OC} = 5V \]
Short Circuit Current

\[ I_{sc} = \frac{5V}{1k\Omega} = 5mA \]
Load line is the line that connects $I_{sc}$ and $V_{oc}$.

$slope = -\frac{1}{R_{Th}}$

The slope of the load line is related to the shunt resistance $R_{Th}$. The load line connects the short-circuit current $I_{sc}$ and the open-circuit voltage $V_{oc}$.
I-V Curve

• Note that if you calculated the open circuit voltage and short circuit current before measuring the I-V characteristic,
  ▫ You can determined:
    • whether you only need to collect the forward bias or reverse bias I-V curve.
    • the settings for the maximum current and voltage range on the curve tracer or semiconductor parameter tester.
      • Curve tracer and semiconductor parameter tester are the names of the two pieces of equipment that are dedicated instruments for measuring I-V curves.
Approach 3:

Piecewise Models

OFF

BREAKDOWN

ON
“ON” Model

\[ V_D \geq V_{on} \]
\[ I_D \geq 0 \text{ mA} \]
“OFF” Model

$V_{BR} < V_D < V_{on}$

$I_D = 0 \text{ mA}$
“BREAKDOWN” Model

\[ V_z = |V_{BR}| \quad V_D \leq V_{BR} \text{ so } V_D \leq -V_z \]

\[ I_Z = I_D \text{ where } I_D < 0 \text{ mA and } I_Z > 0 \text{ mA} \]
Steps in Piecewise Calculations

1. First, determine which model should be substituted for the diode.
2. Calculate the diode voltage and current using the model.
3. Verify that the diode voltage and current are acceptable for the model chosen.
   
   If not, chose another model and try again.
What I do to quickly select models is to try the OFF model first and calculate the diode voltage (which is equal to $V_{OC}$).

From the load line analysis, we know that $V_{OC} = 5\text{V}$.

This is much greater than the built-in voltage so this is the wrong model and the correct one is probably the ON model.
Given:  \( V_{on} = 0.4 \, \text{V} \)
\( Rs = 0 \, \Omega \)

\[
-5V + 1k\Omega \cdot I_D + V_{on} = 0
\]
\[
-5V + 1k\Omega \cdot I_D + 0.4V = 0
\]
\( I_D = 4.6mA \)

The calculated diode current is positive when the turn-on voltage is 0.4V. This is acceptable for the ON model so this model is the correct one to use.
Summary

- There are three different techniques that are used to analyse circuits that contain diodes.
  - **Ideal diode equation** is used when the diode voltage between the breakdown voltage and the turn-on voltage of the diode.
  - **Load line analysis** can be used as long as you have an I-V characteristic for the diode.
  - **Piecewise models** are used to estimate the diode current and voltage.
    - The accuracy depends on the region of operation and the use of the series resistors, $R_s$ and $R_z$. 